A new development cycle of the Statistical Toolkit

To live in the hearts we leave behind is not to die. (T. Campbell)
In memory of Paolo Vairetti.

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Abstract
The Statistical Toolkit (ST) [1, 2] is an open source system specialized in the statistical comparison of distributions. It addresses requirements common to different experimental domains, such as simulation validation (e.g. comparison of experimental and simulated distributions), regression testing in software development and detector performance monitoring.

Various sets of statistical tests have been added to the existing collection to deal with the one sample problem (i.e. the comparison of a data distribution to a function, including tests for normality, categorical analysis and the estimate of randomness). Improved algorithms and software design contribute to the robustness of the results. A simple user layer dealing with primitive data types (e.g. parsing comma-separated-values files) facilitate the use of the toolkit both in standalone analyses and in large scale experiments.

New development cycle
The new development cycle of the ST has been moved to SVN repository. To be as self-consistent as possible, the number of dependencies on external software systems has been minimized. The only proper requirement is the GNU Scientific Library [3]. In order to facilitate running the ST on (wide) variety of operating systems, the Cross Platform Make [4] build system is used. The test testing tool, distributed as a part of CMake, is used for unit testing.

The new development cycle of the toolkit has three different user layers. Without any external dependencies the user layer that reads comma separated list of values (csv ascii files) is built by default. Additional user layers, to AIDA [5] and ROOT [6], facilitating usage of ST objects from the these tools and analysis of data that preexisted distributions. On properly set-up environments, either or both will be found by cmake when user specifies correct variables.

The ST now also comes with an extensive set of unitTests, which are meant to test the consistency of the statistical test for each new version of the ST.

Statistical tests in the ST
The ST started out as a statistical data analysis tool for the problem of comparing two distributions. The first development cycles of the ST delivered a wide set of a goodness-of-fit (GoF) tests, which are suitable for regression testing, validation of simulation to the experimental data, comparison of expected vs. reconstructed distributions and comparison of data from different sources. The collection of implemented tests encompasses:

<table>
<thead>
<tr>
<th>GoF test</th>
<th>Distribution Type</th>
<th>&lt;ComparisonAlgorithm&gt; Class</th>
</tr>
</thead>
<tbody>
<tr>
<td>Anderson-Darling</td>
<td>Binned</td>
<td>AndersonDarlingBinned</td>
</tr>
<tr>
<td></td>
<td>Unbinned</td>
<td>AndersonDarlingUnbinned</td>
</tr>
<tr>
<td>Chi-squared</td>
<td>Binned</td>
<td>Chi2Binned</td>
</tr>
<tr>
<td></td>
<td>Unbinned</td>
<td>Chi2Unbinned</td>
</tr>
<tr>
<td>Fisz-Cramer-von-Mises</td>
<td>Binned</td>
<td>FiszCramervonMisesBinned</td>
</tr>
<tr>
<td></td>
<td>Unbinned</td>
<td>FiszCramervonMisesUnbinned</td>
</tr>
<tr>
<td>Girone</td>
<td>Unbinned</td>
<td>GironeUnbinned</td>
</tr>
<tr>
<td>Goodman</td>
<td>Unbinned</td>
<td>KoldmogorovSmirnovApproximated</td>
</tr>
<tr>
<td>Kolmogorov-Smirnov</td>
<td>Unbinned</td>
<td>KolmogorovSmirnov</td>
</tr>
<tr>
<td></td>
<td></td>
<td>WeightedKolmogorovSmirnov</td>
</tr>
<tr>
<td></td>
<td></td>
<td>WeightedBinnedKolmogorovSmirnov</td>
</tr>
<tr>
<td>Kuiper</td>
<td>Unbinned</td>
<td>KuiperUnbinned</td>
</tr>
<tr>
<td>Tiku</td>
<td>Unbinned</td>
<td>TikuUnbinned</td>
</tr>
<tr>
<td>Watson</td>
<td>Unbinned</td>
<td>WatsonUnbinned</td>
</tr>
</tbody>
</table>

The new development cycle extends the ST with one sample goodness-of-fit tests, i.e. comparing data to reference functions, and tests for randomness. These tests provide complementary information to the existing tests: for instance, tests for randomness can highlight the presence of systematic effects in the distributions subject to comparison, which goodness-of-fit tests cannot detect. The extension of functionality of the ST also includes tests for categorical data. A list of new tests, some of which are already available in the new development version of the ST, is here:

<table>
<thead>
<tr>
<th>Test</th>
<th>Distribution Type</th>
<th>Class</th>
</tr>
</thead>
<tbody>
<tr>
<td>Wald-Wolffowitz runs test</td>
<td>Binned</td>
<td>WaldWolfowitzOneSampleRunsTest</td>
</tr>
<tr>
<td>Wald-Wolffowitz test of randomness</td>
<td>Unbinned</td>
<td>WaldWolfowitzOneRandomnessTest</td>
</tr>
<tr>
<td>Mann-Whitney U test</td>
<td>Binned</td>
<td>MannWhitneyOneSampleTest</td>
</tr>
<tr>
<td></td>
<td>Unbinned</td>
<td>MannWhitneyOneSampleUnbinned</td>
</tr>
<tr>
<td>Fisher’s Exact test</td>
<td></td>
<td>FishersExact2x2Test</td>
</tr>
<tr>
<td>Chi-squared paired test</td>
<td>Paired Values</td>
<td>Chi2CurvComparisonAlgorithm</td>
</tr>
</tbody>
</table>

Example

Is the number of earthquakes per year a random number?

We have two data samples. If the differences between the two were due only to statistical fluctuations, one would expect the differences to be a rather large number of short sequences (runs) of consecutive positive and negative values. Using Wald-Wolffowitz runs test [8] one can infer some systematic effects between the two samples. One can use the runs test to test the randomness of the numerical data around some given value (or function).

Importing the data from comma separated list of values (csv ascii file)

```cpp
CsvReader* reader = new CsvReader();
data->setDelimiter(‘‘);
default delimiter is comma
read only second column (column numbers start from 0)
data->readColumnsFromFile(‘earthquakes.csv’);
```

Construct OneDimData object, and make it binary around mean value

```cpp
OneDimData numData(numData->getDbData());
//construct one (dimensional data)
num.Print();
//print data
num.makeBinary(numData->getMean());
//make runs around mean
num.Print();
```

Run the Wald-Wolfowitz runs test and get the results

```cpp
WaldWolfowitzOneSampleRunsTest* test = new WaldWolfowitzOneSampleRunsTest();
vector<signed> w = test->calculate(num);
count<“<” = w << c.wav.at(0)<<endl;
(calculate p-value of
count<“<” = w << c.wav.at(1)<<endl;
//number of elements of first
calculate p-value for
count<“<” = w << c.wav.at(2)<<endl;
//number of runs

The results: m = 52
A = 31
```

Calculate the p-value from given test results

```cpp
WaldWolfowitzQualityChecker* qc = new WaldWolfowitzQualityChecker();
ComparisonResult result = qc->compare(ww);
```

```cpp
result = result<<”<”<<resultQty<<endl;
```

The calculated p-value is 0.00011. So: can we answer the question? No. But we can say that the exact p-value is small enough to have strong statistical evidence to reject the null hypothesis that in the 20th century, the number of earthquakes with magnitude above 7.0 is not randomly distributed around their mean value.

Bibliography